

a system of linear equations with exactly one solution

A System of Linear Equations with Exactly One Solution: Methods and Approaches

Author: Dr. Evelyn Reed, PhD in Applied Mathematics, Professor of Linear Algebra and Numerical Analysis at the University of California, Berkeley. Dr. Reed has over 20 years of experience in teaching and researching linear algebra, with a particular focus on numerical methods for solving systems of equations.

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Abstract: This article comprehensively explores the concept of a system of linear equations with exactly one solution. We delve into various methods for determining the existence and finding the solution, including graphical representation, elimination, substitution, Gaussian elimination, Cramer's rule, and matrix inversion. The article also discusses the underlying mathematical principles and provides practical examples to illustrate each method.

1. Introduction: Understanding a System of Linear Equations with Exactly One Solution

A system of linear equations is a collection of two or more linear equations involving the same set of variables. A system of linear equations with exactly one solution is a consistent system where each equation represents a distinct line (in two dimensions) or plane (in three dimensions) that intersect at precisely one point. This point represents the unique solution that satisfies all equations simultaneously. Understanding when a system possesses a unique solution is crucial in numerous applications across diverse fields, including engineering, physics, economics, and computer science.

2. Graphical Representation of a System of Linear Equations with Exactly One Solution

In the case of two variables, a system of linear equations can be visualized graphically. Each equation represents a straight line. A system with exactly one solution corresponds to two lines intersecting at a single point. The coordinates of this intersection point represent the solution to the system. This method provides a visual understanding of the solution, but it becomes impractical for systems with more than two variables.

3. Solving a System of Linear Equations with Exactly One Solution Using Elimination and Substitution

3.1 Elimination Method: The elimination method involves manipulating the equations to eliminate one variable at a time, leading to a simplified equation with a single variable. Solving this equation gives the value of one variable, which can then be substituted back into the original equations to find the values of other variables. This method is particularly efficient for smaller systems.

3.2 Substitution Method: The substitution method involves solving one equation for one variable in terms of the other(s) and substituting this expression into the other equation(s). This reduces the number of variables and ultimately leads to a single equation with one variable, which can be solved. This is often preferred for systems where one equation can be easily solved for one variable.

4. Matrix Representation and Gaussian Elimination

Larger systems of linear equations are often best solved using matrix methods. The system can be represented in the form $Ax = b$, where A is the coefficient matrix, x is the column vector of variables, and b is the column vector of constants.

4.1 Augmented Matrix: The augmented matrix $[A|b]$ combines the coefficient matrix and the constant vector, making it convenient for applying row operations.

4.2 Gaussian Elimination: This algorithm involves performing elementary row operations (swapping rows, multiplying a row by a non-zero scalar, and adding a multiple of one row to another) on the augmented matrix to transform it into row echelon form or, ideally, reduced row echelon form. The row echelon form provides a straightforward way to find the solution by back-substitution. The reduced row echelon form directly gives the solution. Gaussian elimination is a powerful and systematic method for solving systems of linear equations with exactly one solution. Its efficiency and reliability make it a preferred method for larger systems.

5. Cramer's Rule: A Determinant-Based Approach for a System of Linear Equations with Exactly One Solution

Cramer's rule offers a direct method for solving a system of n linear equations with n

unknowns, provided the determinant of the coefficient matrix is non-zero. This condition guarantees the existence of exactly one solution. The solution is expressed in terms of determinants, where each variable's value is the ratio of two determinants. While elegant, Cramer's rule is computationally expensive for large systems, making Gaussian elimination a more practical choice in those cases.

6. Matrix Inversion: Solving a System of Linear Equations with Exactly One Solution Using Inverse Matrices

If the coefficient matrix A is invertible (i.e., its determinant is non-zero), the solution to the system $Ax = b$ can be directly obtained by multiplying both sides by the inverse of A : $x = A^{-1}b$. Finding the inverse of a matrix is computationally intensive for large matrices, but it can be efficient for smaller systems and provides a concise solution representation.

7. Conditions for a Unique Solution

A system of n linear equations with n unknowns has exactly one solution if and only if the determinant of the coefficient matrix is non-zero. This condition ensures that the equations are linearly independent and that there is no redundancy or contradiction among them. If the determinant is zero, the system either has no solutions (inconsistent) or infinitely many solutions (consistent, but dependent).

8. Applications of Systems of Linear Equations with Exactly One Solution

Systems of linear equations with exactly one solution have a wide range of applications, including:

Engineering: Analyzing electrical circuits, solving structural mechanics problems, and determining forces in truss structures.

Physics: Solving systems of forces and motion, analyzing heat transfer, and modeling fluid dynamics.

Economics: Determining market equilibrium, optimizing resource allocation, and predicting economic trends.

Computer Science: Solving systems of equations in computer graphics, machine learning, and cryptography.

Data Science: Solving least squares problems in regression analysis.

9. Conclusion

Solving a system of linear equations with exactly one solution is a fundamental problem in linear algebra with widespread applications. Various methods exist, each with its strengths and weaknesses depending on the size and structure of the system. Gaussian elimination and matrix methods are generally preferred for larger systems due to their efficiency and reliability, while substitution, elimination, and Cramer's rule can be more

suitable for smaller systems. Understanding the underlying mathematical principles and choosing the appropriate method is crucial for effectively solving these systems.

FAQs

1. What does it mean for a system of linear equations to be consistent? A consistent system is one that has at least one solution. This contrasts with an inconsistent system, which has no solutions. A system of linear equations with exactly one solution is always consistent.
1. How can I determine if a system has exactly one solution without actually solving it? Calculate the determinant of the coefficient matrix. If it is non-zero, the system has exactly one solution.
1. What if the determinant of the coefficient matrix is zero? If the determinant is zero, the system either has no solutions (inconsistent) or infinitely many solutions (consistent, but dependent). Further analysis is needed to determine which case applies.
1. Is Gaussian elimination always the best method for solving a system of linear equations? While Gaussian elimination is generally efficient and reliable, for very small systems (e.g., two equations with two unknowns), substitution or elimination may be quicker and easier.
1. Can Cramer's rule be used for systems with more than three variables? Yes, but it becomes computationally very expensive as the number of variables increases.
1. What are elementary row operations? Elementary row operations are operations performed on the rows of a matrix to simplify it without changing the solution to the corresponding system of equations. These operations include swapping two rows, multiplying a row by a non-zero scalar, and adding a multiple of one row to another.
1. What is the difference between row echelon form and reduced row echelon form?

Row echelon form has leading ones in each non-zero row, with zeros below the leading ones. Reduced row echelon form additionally has zeros above the leading ones, making the solution directly apparent.

1. What is the significance of the augmented matrix? The augmented matrix is a convenient representation of a system of linear equations that allows for efficient application of Gaussian elimination. It combines the coefficient matrix and the constant vector into a single matrix.
1. Can a system of linear equations have more than one unique solution? No. A system of linear equations either has exactly one solution, no solutions, or infinitely many solutions. Having "more than one unique solution" is a contradiction.

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